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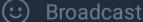
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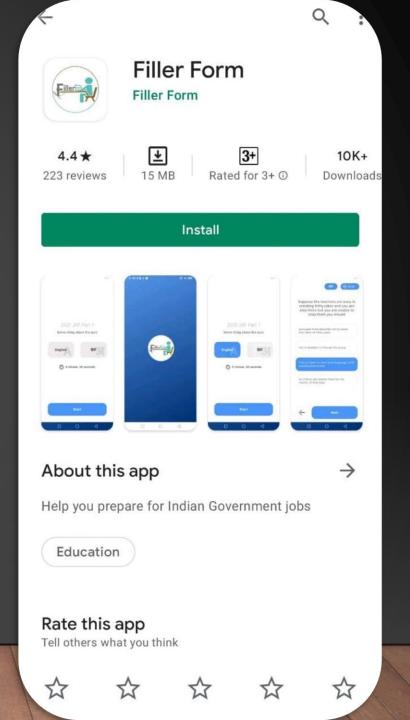
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# □ Discrete Structure and Optimization

### Content:

- Boolean Algebra (part 1)
- 2) Basic operation
- 3) Logic gates
- 4) Duality



# Properties of Boolean Algebra

# 1. Commutative Properties:

$$(i)a+b = b+a$$

$$(ii)a*b=b*a$$

# 2. Distributive Properties

(i) 
$$a+(b*c)=(a+b)*(a+c)$$

$$(ii)a*(b+c)=(a*b)+(a*c)$$

# 3. Identity Properties

(i) 
$$a+0=a$$

(ii) 
$$a *1=a$$

# 4. Complemented Laws:

(i) 
$$a+a'=1$$

(ii) 
$$a * a' = 0$$

# **Idempotent Laws**

$$(i)a+b=a$$

(ii) 
$$a * a = a$$

# **Absorption Laws**

$$(i)a + (a*b) = a$$

### **Boundedness laws**

$$a + 1 = 1$$

$$a.0 = 0$$

### Associative laws:

$$(a + b) +c = a+(b+c)$$
  
 $(a.b).c =a.(b.c)$ 

# **Uniqueness of complement:**

$$a + x = 1$$
 and  $ax = 0$ , then  $x = a'$ 

### De-Morgan's laws:

$$(a +b)' = a'.b'$$
  
 $(a.b) = a' +b'$ 

# Involution law:

**b.** 
$$0' = 1$$

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# Logic Gates and Circuits:

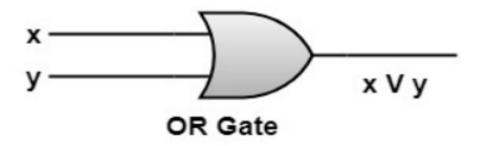
**AND Gate:** An AND gate receives inputs x and y and produces output denoted x  $\land$  y, as shown in logic table

x	y	x^ y
0	0	0
0	1	0
1	0	0
1	1	1



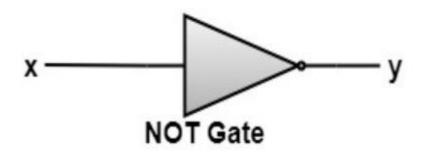
**OR Gate:** An OR gate receives inputs x and y and produces output denoted x V y as shown in the logic table

x	y	x^ y
0	0	0
0	1	1
1	0	1
1	1	1



**NOT Gate:** A NOT Gate receives input x and produces output y denoted x' as shown in the logic table

x	x'	
0	1	
1	0	

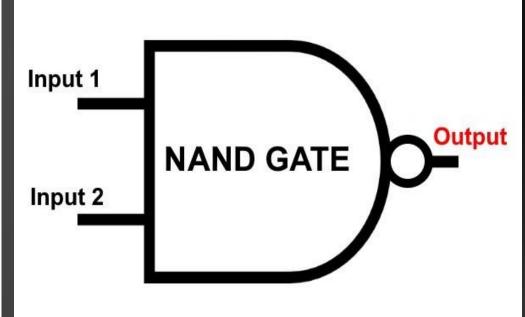


We can interconnect these devices to form an electronic circuit that realizes any given Boolean Expression.

### NAND Gate

A NAND gate is a logic gate that gives a low output only if all its inputs are high, otherwise it gives high output.

Α	В	~(A.B)
0	0	1
0	1	1
1	0	1
1	1	0

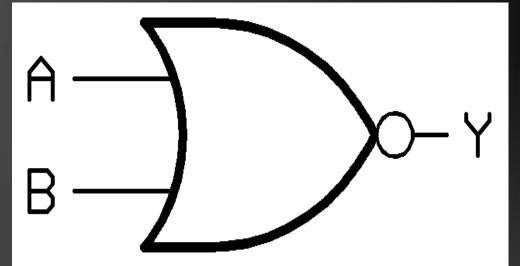


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### **NOR Gate**

An NOR gate is a logic gate that gives high output if both the inputs are low, otherwise it gives low output.

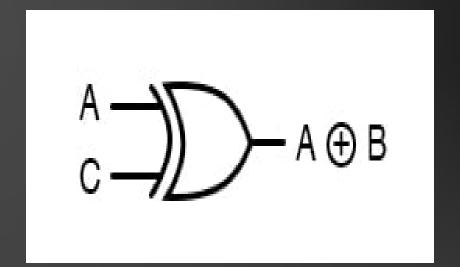
Α	В	~(A+B)
0	0	1
0	1	0
1	0	0
1	1	0



### XOR (Exclusive OR) Gate

An XOR gate is a logic gate that gives high output if the inputs are different, otherwise it gives low output.

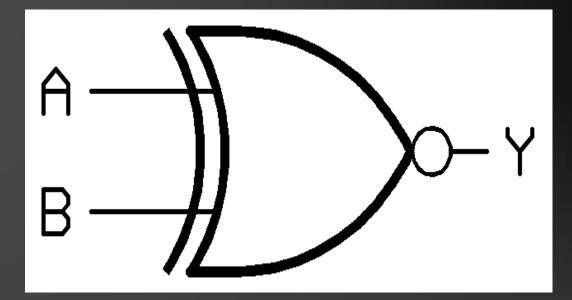
Α	В	A⊕B
0	0	0
0	1	1
1	0	1
1	1	0



### X-NOR (Exclusive NOR) Gate

An EX-NOR gate is a logic gate that gives high output if the inputs are same, otherwise it gives low output.

Α	В	A X-NOR B
0	0	1
0	1	0
1	0	0
1	1	1



# Theorems of Boolean Algebra

The following two theorems are used in Boolean algebra.

- Duality theorem
- DeMorgan's theorem

### **Duality Theorem**

This theorem states that the **dual** of the Boolean function is obtained by interchanging the logical AND operator with logical OR operator and zeros with ones. For every Boolean function, there will be a corresponding Dual function.

Let us make the Boolean equations relations that we discussed in the section of Boolean postulates and basic

laws into two groups. The following table shows these two groups.

Group1	Group2
x + 0 = x	x.1 = x
x + 1 = 1	x.0 = 0
x + x = x	x.x = x
x + x' = 1	x.x' = 0
x + y = y + x	x.y = y.x
x + y + z = x + y + z	x. y.z = x.y.z
x. y + z = x.y + x.z	$x + y \cdot z = x + y \cdot x + z$ Activate Windows



Operator / Variable	Dual
AND	OR
OR	AND
1	0
0	1

### REMEMBER THIS

- 1) 0 WILL BE CHANGE TO 1
- 2) 1 WILL BE CHANGE TO 0
- 3) AND WILL BE CHANGE TO OR
- 4) OR WILL BE CHANGE TO AND

### DeMorgan's Theorem

This theorem is useful in finding the **complement of Boolean function**. It states that the complement of logical OR of at least two Boolean variables is equal to the logical AND of each complemented variable.

DeMorgan's theorem with 2 Boolean variables x and y can be represented as

$$x+y$$
 '= x'.y'

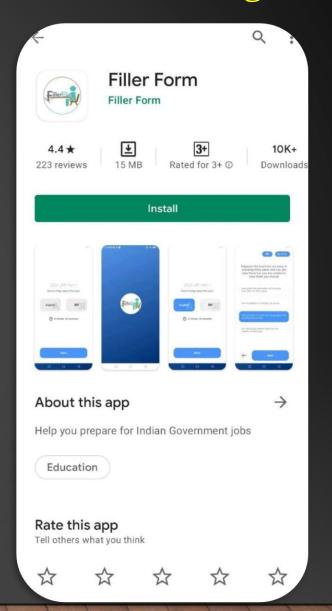
The dual of the above Boolean function is

$$x.y$$
 '= x' + y'

Therefore, the complement of logical AND of two Boolean variables is equal to the logical OR of each complemented variable. Similarly, we can apply DeMorgan's theorem for more than 2 Boolean variables also.

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